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# Bit Reversal Broadcast Scheduling for Ad Hoc Systems

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# How to broadcast efficiently?



## Broadcasting in ad hoc systems

- a shared radio channel for all receivers
- time division
- unpredictable what is to be sent to to whom
- the receivers may come and go

## Targets

- robustness
- no a priori knowledge necessary
- easy adjustment
- energy efficiency



# Remote management of a sensor network

application scenario

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## Wireless sensor network

- sensors in inaccessible places
- battery operated, exchanging batteries very problematic
- sensor field management via a broadcasting channel
- event driven activities
- frequently: the sensors have to sleep almost all the time

## Design goals

- the sensor field should work as long as possible
- most energy are used for keeping antenna active
- **switch off the antenna whenever possible**



# Ad hoc network for security/ disaster recovery

## application scenario

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### Technical issues

- mobility of receivers
- information critical - if a receiver is in the broadcasting range, **it must not skip any message designated to it**
- energy should be saved – problem of exhausting batteries
- emergency situations are non typical - no a priori knowledge and no a priori set up

### targets

- the receiver can emerge at any moment
- no message lost, but the antennas deactivated whenever almost all the time
- overhead due to message headers should be relatively small



# Sharing frequencies

application scenario

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## Broadcasting services and local communication

creating local subnetworks:

- take advantage of signal propagation decay: a weak but close sender can be better heard as remote strong station
- local network may reuse the broadcast frequency
- local subnetwork sending locally a weak signal on the broadcast frequency – whenever not receiving data from the broadcaster

## Targets

- good time synchronization despite unpredictable a priori broadcast destinations



# Naïve solution

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## Simple inefficient solution

- broadcast cycle consisting of a fixed number of fixed size slots
- each slot starts with destination address/key
- the messages sent in the order corresponding to the keys

slot<sub>1</sub>: key<sub>1</sub> | data<sub>1</sub>

slot<sub>2</sub>: key<sub>2</sub> | data<sub>2</sub>

...

slot<sub>k</sub>: key<sub>k</sub> | data<sub>k</sub>



# Naïve solution

disadvantaged

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slot<sub>1</sub>: key<sub>1</sub> | data<sub>1</sub>  
slot<sub>2</sub>: key<sub>2</sub> | data<sub>2</sub>  
...  
slot<sub>k</sub>: key<sub>k</sub> | data<sub>k</sub>

## Problems

- a receiver has to listen all the time, until the key becomes higher
- the worst case: listening the whole cycle
- the messages to one receiver comes in a contiguous interval  
being late or burst error  $\Rightarrow$  the whole transmission lost





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# RBO

## Broadcasting with Reversed Binary Ordering



# Bit reversal

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## Bit reversal

If  $t$  is a  $k$ -bit number, then  $\text{rev}_k(t)$  is the  $k$ -bit number with the same representation, but written in a reverse order.

e.g.

$$\text{rev}_5(00001) = 10000$$

$$\text{rev}_5(00010) = 01000$$

$$\text{rev}_5(11000) = 00011$$



# Bit Reversal Scheduling

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## Scheduling

- 1 keys after sorting:  $a_1, \dots, a_k$
- 2 **the message with the key  $a_i$  is sent at the slot**

$$\text{rev}_k(i)$$



# RBO Scheduling

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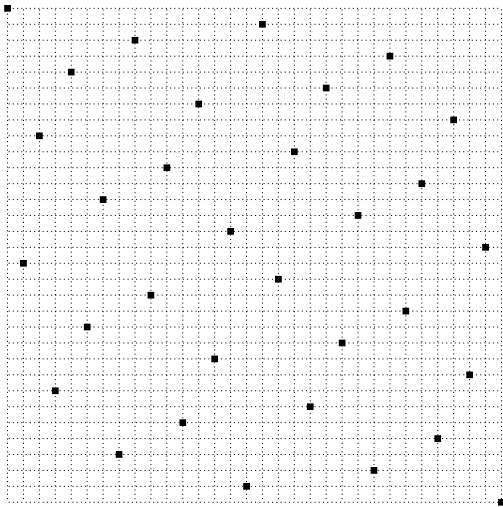
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y axis: time, x axis: position  $i$  in the sorted sequence



# RBO Scheduling

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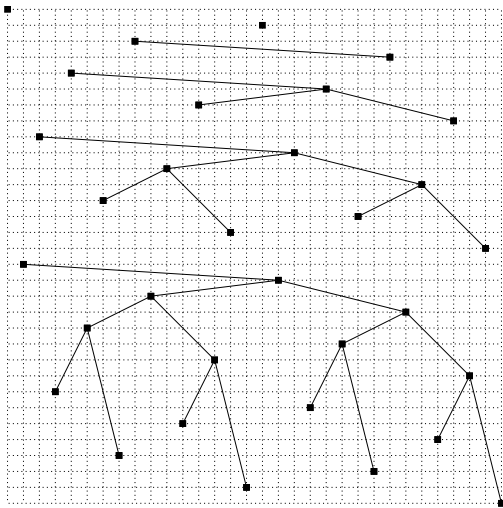
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y axis: time, x axis: position  $i$  in the sorted sequence



# RBO -main properties

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## Data model

- a message to be sent in one slot consists of
  - a key
  - data
- a receiver is interested in messages with keys from some **interval**
- the intervals of different receivers may overlap



# RBO -main properties

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## Data model

- a message to be sent in one slot consists of
    - a key
    - data
  - a receiver is interested in messages with keys from some **interval**
  - the intervals of different receivers may overlap
- 
- intervals enable to send longer data with fixed size slots
  - intervals may be related to location of a receiver or its function
  - a receiver may be interested in more than one interval



# Receiver algorithm

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## Challenge

- the keys for the messages sent during a cycle are unknown for the receiver
- based on the messages received so far, the receiver has to determine which slots to skip

## Idea

- a receiver interested in interval  $J$  holds
  - a lower bound  $lb$
  - an upper bound  $ub$for indexes  $i$  such that  $a_i$  holds the key from  $J$
- after slot is received and the key is not from  $J$ , then  $lb$  or  $ub$  may be updated



# Receiver algorithm

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- in time-slot  $t$ , if  $lb \leq \text{rev}_k(t) \leq ub$ , then the receiver activates the antenna and gets a message with key  $\kappa = \kappa_{\text{rev}_k(t)}$ .
- Updating  $lb$  and  $ub$ : according to the value of  $\kappa$ :
  - Case 1 if  $\kappa < \kappa'$ , then  $lb := \text{rev}_k(t) + 1$ ,
  - Case 2 if  $\kappa'' < \kappa$ , then  $ub := \text{rev}_k(t) - 1$ ,
  - Case 3 if  $\kappa' \leq \kappa \leq \kappa''$ , then proper message received
- If after the update  $lb > ub$ , then there is no message with a key from  $J$  in the current broadcast cycle and the receiver switches off its antenna.



# Correctness

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No message from the range is skipped  
follows immediately by the construction

Computational complexity

- simple and short program computing bit reversal
- trial implementation on TinyOS works fine

efficient Java implementation available from Marcin Kik



# Efficiency

what is the number of updates of lb and ub small?

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## Remarkable properties of RBO

- 1 the ordering of positions sent is that the new points come always almost in the middle between the closest positions already sent
- 2 self similarity: if the receiver starts not at the beginning of the broadcast cycle, then almost the same structure can be observed



# RBO - Binary search structure

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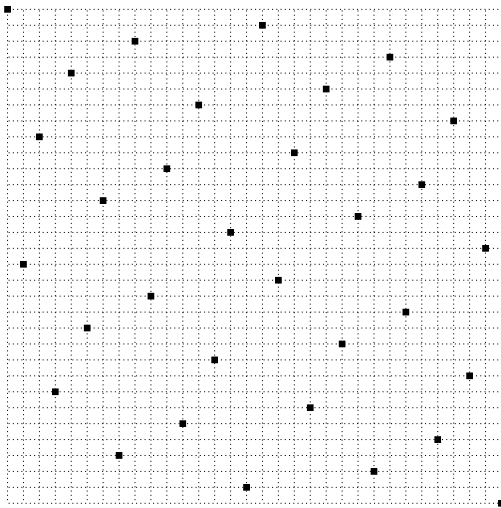
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y axis: time, x axis: position  $i$  in the sorted sequence



# RBO Scheduling

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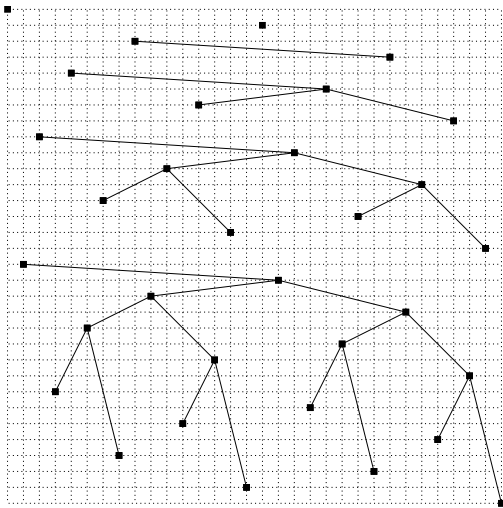
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$y$  axis: time,  $x$  axis: position  $i$  in the sorted sequence



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# Analysis



# Problem

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## Energy efficiency

- **What is the number of time slots that the receiver listens to the channel, but the key is outside the target interval?**  
*(it is used merely for updating lb and ub)*
- the number of these time slots is called **extra energy**



# Lower bound for extra energy

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## Lower bound

- There are examples showing that for a cycle consisting of  $2^k$  slots extra energy is  $2k - 1$ .
- intuitively:  $k$  time slots might be necessary to find the starting position of keys from  $J$  in the sorted sequence of keys.
- Analogously,  $\log_2(2^k) = k$  steps might be needed to find the upper part.





# Upper bound

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## Problems

- this is NOT exactly the binary search tree,
- one can show some cases when there is no “halving effect”
- what if the receiver starts not at the beginning of the cycle?
  - the *binary tree structure* gets complicated



# Upper bound

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## Problems

- this is NOT exactly the binary search tree,
  - one can show some cases when there is no “halving effect”
  - what if the receiver starts not at the beginning of the cycle?
    - the *binary tree structure* gets complicated
- 
- It is relatively easy to show that the extra energy is something like  $4k$  for cycle of length  $2^k$ .
  - Trial executions all have shown a much better behavior. So what is the real energy cost (extra energy)?



# Main Result

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## Main Theorem

The extra energy of RBO protocol is at most  $2k + 3$  for any input configuration.



# Remarks about the proof

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## 1 look into proceedings:

- the proof is extremely long
- one of the difficulties is the extremely large number of different notions necessary to carry out the proof
- the proof has been remarkably simplified compared to the first version

... but still it requires a big effort to follow it.



# Remarks about the proof

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## 1 look into proceedings:

- the proof is extremely long
- one of the difficulties is the extremely large number of different notions necessary to carry out the proof
- the proof has been remarkably simplified compared to the first version

... but still it requires a big effort to follow it.

## 2 What is the minimal size/ combinatorial complexity of the proof for (nice) behavior of this simple protocol?



# Left energy versus right energy

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## Hope

One may expect that there is some symmetry and it suffices to estimate the number of updates of  $lb$  or  $ub$  to get the result.



# Left energy versus right energy

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## Hope

One may expect that there is some symmetry and it suffices to estimate the number of updates of  $lb$  or  $ub$  to get the result.

## The hope is wrong

Estimating the number of cases of updating  $ub$  (*right energy*) is much more complicated than the case of updating  $lb$  (*left energy*).

**There are many very subtle effects.**



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## However it works!

You do not have to recheck the proof to take advantage of good properties of the RBO scheduling





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# Extensions



# Fault model - random errors

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## Random errors

- it may happen that due to propagation problems the receiver may not read some slots
- this occurs in particular when the energy level of the signal is low



# Fault model - random errors

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## Random errors

- it may happen that due to propagation problems the receiver may not read some slots
- this occurs in particular when the energy level of the signal is low

## Behavior of RBO for random errors

- the receivers might be forced to spend more extra energy
- corresponds roughly to a binary search tree where we do not know the outcome on some nodes



# Fault model - burst errors

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## burst errors

- due to some external sources during a short period of time all time slots are scrambled
- this occurs in particular due to shortcuts (trains, trams, ...), vehicles passing by and reflecting the waves, ... or some local problems of the receiver



# Fault model - burst errors

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## burst errors

- due to some external sources during a short period of time all time slots are scrambled
- this occurs in particular due to shortcuts (trains, trams, ...), vehicles passing by and reflecting the waves, ... or some local problems of the receiver

## Behavior of RBO for burst errors

- bit reversal converts local error concentrated on an interval to single errors dispersed evenly over the whole interval



# Streaming multiple video channels

one more application

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How to organize assignment of time slots for video channels?

the scheme should be

- simple
- flexible (any division of time available to different video channels)
- relatively tolerant to burst errors



# Streaming multiple video channels

one more application

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How to organize assignment of time slots for video channels?

the scheme should be

- simple
- flexible (any division of time available to different video channels)
- relatively tolerant to burst errors

RBO solution

- assign each channel an interval, e.g.  $[i, i + 1, \dots, i + \Delta]$
- send slot  $i$  at time  $\text{rev}(i)$
- thereby the time channels are evenly dispersed
  - good because of burst errors
  - good for weak receiver devices - giving them time between consecutive frames



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# Thanks for your attention!

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