

Segment Document Protection

Kutyłow Gebal

Introductio

Key Structures

Tree-Based Key

Sequential Key

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Optimizing Segment Based Document Protection

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Segment Based Document Protection

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Segmented Document Key Structures

Tree-Based Key Derivation

Sequential Key Derivation

inal remark

Motivation

- For confidentiality, data in a digital document may be encrypted
 - then only a reader with the decryption key may read it.
- However, not all information are equally confidential: for each part there is a different subset of people that have the right to read it.
- Auxiliary right management information can be nicely encoded in an XML-structure of a document.
- The things might become messy:
 many different document user profiles, each profile defining the read access right for all parts of the document.



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Trivial solution

use a different encryption key for each part (segment)

Disadvantage

if a user has the right to many segments, then many keys must be given to him.

$$A = \{K_1, K_2, K_3, K_4, K_5, K_6, K_8\}$$

$$B = \{K_2, K_4, K_5, K_7, K_8\}$$

$$C = \{K_3, K_5, K_6, K_7, K_8\}$$

$$D = \{K_4, K_7\}$$



Segment Based Document Protection access graph for a document

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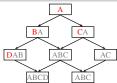
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Access graph G

- Nodes of *G* segments of the document.
- There is an arc AB in G, if all users having access right to A have also access right to B.
- Each node is labeled by the key used to encrypt that segment.

Well designed G is acyclic.

A user having access right to a segment *A* has also access right to every *B* such that there is a directed path from *A* to *B*.





Dags and Key Derivation Techniques one-way derivation of keys

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Goal

reduce the number of keys that need to be given to a user.

Linear scheme

If the access graph defines a linear ordering $A_1 \succeq A_2 \succeq \ldots \succeq A_m$, then the corresponding keys may be derive with any one-way (hash) function H. Choose a key K_1 at random and for $i=2,\ldots,m$ derive

$$K_i \leftarrow H(K_{i-1})$$

Advantage

It suffices to give a user the key K_i , where i is the smallest number such that the user has the access right to A_i .



Dags and Key Derivation Techniques

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Tree schemes

If the access graph is a tree, then a similar solution applies:

If a node A has child nodes $B_1, \ldots B_k$ and a key K has been assigned to A, then to B_i ($i \le k$) we assign the key

$$K_i \leftarrow H(i, K)$$



Dags and Key Derivation Techniques schemes for arbitrary dag

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Arbitrary dags - technique 1

For a dag P describing the access rights find a mapping $\rho: P \to N$, such that $A \succeq B$ iff $\rho(A)|\rho(B)$.

Use a multiplicative group \mathbb{G} such that computing the roots in \mathbb{G} is infeasible (e.g. use RSA Assumption).

Choose an element $g \in \mathbb{G}$, and compute $K_A \leftarrow g^{\rho(A)}$ as the key for node A.

If $\rho(A)|\rho(B)$, then $K_B \leftarrow K_A^{\rho(B)/\rho(A)}$.

Disadvantages: high computational complexity, low flexibility.



Dags and Key Derivation Techniques schemes for arbitrary dag

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Arbitrary dags - technique 2

- Use an arbitrary tree scheme this leads to conflicts when a node v has more than one incoming arcs.
- If the key of node C should be K_C and the computation for an arc (B, C) yields K_B , then define the offset for arc BC as K_C xor $H(K_B)$. Then:

$$K_C = H(K_B)$$
 xor offset for BC

The offset is the public information corresponding to the arc included in the document.

$$egin{array}{c|cccc} A & B & & & & & & \\ \hline K_C = H(K_A) & C & K_C = H(K_B) \ xor \ K' & & & & & \\ \hline \end{array}$$



Problem Statement

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In the segmented document we have to describe:

- key derivation method for each arc of the access graph,
- offset, if it is necessary for a given arc.

Our goal

Find solution with low space overhead of the document encoding and small computational requirements.

Eliminate as many offsets as possible!



Problem Statement

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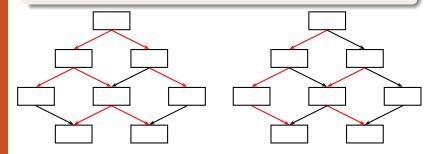
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Idea:

for tree method: embed a tree or disjoint trees in *G* for path method: embed a path or disjoint paths in *G* and use the offsets only for those edges that are not covered by the embedding.





Problem Statement

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Problem 1

Given a dag G, embed some number of trees in G so that

- the embedded trees are node disjoint,
- the number of arcs that do not belong to any of embedded trees is minimal.

Problem 2

Given a dag G, embed some number of paths in G so that

- the embedded paths are node disjoint,
- the number of arcs that do not belong to any of embedded paths is minimal.



Tree-Based Key Derivation algorithm

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Input: a dag G

Output: a subgraph G' of G that consists a set of disjoint trees and containing the maximal possible number of arcs

Algorithm: Construct a reduced graph G', a subgraph of G, in the following way:

for each node $v \in G$ of indegree greater than 1 pick up an arbitrary arc with endpoint v and remove all other arcs with endpoint v.

Proposition 1

The number of arcs in G' does not depend on choices done during algorithm execution. Moreover, no forest embedded in G may contain more arcs than G'.

So for the tree method, finding an optimal embedding is straightforward.



Sequential Key Derivation situation

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for paths the greedy algorithm mail fail to find an optimal solution:









Sequential Key Derivation algorithm

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The problem can be solved by finding a **minimal vertex-disjoint path cover** in a directed acyclic graph.

A vertex-disjoint path cover in a DAG G = (V, E) is a set of paths P such that every vertex in V is included in exactly one path in P. Paths may start and end anywhere, and they may be of any length, including 0. A minimum path cover of G is a path cover containing the fewest possible paths (i.e. maximum possible edges).

Solution by reduction to **maximum flow problem** thus complexity O(|V||E|).



Final Remarks open problems

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Taking frequency into account

Known: the fraction of users that will have access to a given

node of the access graph.

Process: for each user create the subdocument with only

those segments that are accessible by him

Optimization: minimize the total volume of subdocuments

Tree-based scheme

The modified algorithm selects an arc with endpoint v which is used most frequently. **This constructs an optimal solution.**



Final Remarks open problems

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Sequential scheme - open question

A similar argument cannot be used for finding optimal paths.

The reason: selecting an arc in our scheme does not change the number of arcs in the optimal solution, but changes a lot the shape of all paths in the final solution. As each decision has global consequences, it is unclear how to make an optimal choice.

Solution

Solution by reduction to **maximum weighted bipartite matching** thus complexity $O(|V|^2|E|)$.



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Thanks for your attention!